Math 7350 @ LSU
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Midterm Exam Preparation
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Think about these problems as preparation for the midterm exam.

1. Let $P(z)$ and $Q(z)$ be polynomials.
a. On which (not necessarily simply connected) domains in the complex plane does the expression

$$
\left(\frac{P(z)}{Q(z)}\right)^{1 / n} \quad(n \in \mathbb{N})
$$

define a single-valued analytic function?
b. How can one compute appropriate integrals of the form

$$
\begin{equation*}
\int_{a}^{b}\left(\frac{P(x)}{Q(x)}\right)^{1 / n} d x \tag{1}
\end{equation*}
$$

in which the coefficients of $P$ and $Q$ are real?
2. Think about the inverse Fourier transform of the function

$$
\begin{equation*}
\hat{f}(\omega)=\frac{1}{\omega^{2}+2 i b \omega-1} \tag{2}
\end{equation*}
$$

and what people could do with it.
3. Practice problems like Exercises 8-10 (p. 155) of Chapter 5 of our text book.

