Math 7350 @ LSU Stephen Shipman Midterm Exam Preparation Fall, 2013

Think about these problems as preparation for the midterm exam.

1. Let P(z) and Q(z) be polynomials.

a. On which (not necessarily simply connected) domains in the complex plane does the expression

$$\left(\frac{P(z)}{Q(z)}\right)^{1/n} \qquad (n \in \mathbb{N})$$

define a single-valued analytic function?

b. How can one compute appropriate integrals of the form

$$\int_{a}^{b} \left(\frac{P(x)}{Q(x)}\right)^{1/n} dx, \qquad (1)$$

in which the coefficients of P and Q are real?

2. Think about the inverse Fourier transform of the function

$$\hat{f}(\omega) = \frac{1}{\omega^2 + 2ib\,\omega - 1}\tag{2}$$

and what people could do with it.

3. Practice problems like Exercises 8–10 (p. 155) of Chapter 5 of our text book.