

STUDENT NAME:

Calculus 1550, section 20. Tuesday, October 29, 2003. Twentieth quiz

Use L'hopital's rule to find the following limits. 2 points each.

$$1. \lim_{x \rightarrow \infty} \frac{x^3 + 1}{2x^3 + x} = \lim_{x \rightarrow \infty} \frac{3x^2}{6x^2 + 1} = \lim_{x \rightarrow \infty} \frac{6x}{12x} = \lim_{x \rightarrow \infty} \frac{6}{12} = \frac{6}{12} = \frac{1}{2}$$

↑ l'hopital
↑ l'hopital
↑ cancellation of x
↑ limit of constant is constant

$$2. \lim_{x \rightarrow \infty} \frac{e^{3x-1}}{x} = \lim_{x \rightarrow \infty} \frac{3e^{3x-1}}{1} = \lim_{x \rightarrow \infty} 3e^{3x-1} = \infty$$

↑ l'hopital
(3 = (3x-1)')

Since as $x \rightarrow \infty$
 $3x-1 \rightarrow \infty$,
 and so $e^{3x-1} \rightarrow \infty$.

$$3. \lim_{x \rightarrow 0} \frac{1 - \cos(x)}{\sin(x)} = \lim_{x \rightarrow 0} \frac{\sin(x)}{\cos(x)} = \lim_{x \rightarrow 0} \tan(x) = 0$$

↑ l'hopital
↑ "simplification" (or defⁿ of tan)
↑ fact that if f(x) is continuous at a, then $\lim_{x \rightarrow a} f(x) = f(a)$

$$4. \lim_{x \rightarrow 1} \frac{e^x - e}{x - 1} = \lim_{x \rightarrow 1} \frac{e^x}{1} = e^1 = e$$

↑ l'hopital
↑ if f(x) cont at a, $\lim_{x \rightarrow a} f(x) = f(a)$

for g(x) form, take log first: $y = x^{1/x} \Rightarrow \ln y = 1/x \ln x$

$$2) \text{ take limit } \lim_{x \rightarrow \infty} \frac{\ln x}{x} = \lim_{x \rightarrow \infty} \frac{1/x}{1} = \lim_{x \rightarrow \infty} \frac{1}{x} = 0$$

↑ l'hopital

$$3) \ln y \rightarrow 0, \text{ so } y = e^{\ln y} \rightarrow e^0 = 1, \text{ so } \lim_{x \rightarrow \infty} x^{1/x} = 1$$