Section 1.8 Absolute Value Equations

Review of the Definition of Absolute Value and its Properties

See Section R.2, objective 4 in the etext for an in depth review.

Objective 1: Solving an Absolute Value Equation

The absolute value of a number x, written as |x|, represents the **distance** from a number x to 0 on the number line. Consider the equation |x| = 5. To solve for x, we must find all values of x that are 5 units away from 0 on the number line. The two numbers that are 5 units away from 0 on the number line are x = -5 and x = 5 as shown in the figure below. Therefore, the solution set for |x| = 5 is $\{-5,5\}$.



In general, if u is an algebraic expression and c is a positive real number, then |u|=c is equivalent to u=c or u=-c.

When solving an absolute value equation or inequality, it is necessary to first isolate the absolute value expression.