7.5 Inverse Trigonometric Functions II

OBJECTIVE 1: Evaluating Composite Functions Involving Inverse Trigonometric Functions of the Form $f \circ f^{-1}$ and $f^{-1} \circ f$

Cancellation Equations for the Restricted Sine Function and its Inverse $\sin(\sin^{-1} x) = x$ for all x in the interval [-1,1] $\sin^{-1}(\sin \theta) = \theta$ for all θ in the interval $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$.

Cancellation Equations for the Restricted Cosine Function and its Inverse $\cos(\cos^{-1} x) = x$ for all x in the interval [-1,1] $\cos^{-1}(\cos\theta) = \theta$ for all θ in the interval $[0,\pi]$.

Cancellation Equations for the Restricted Tangent Function and its Inverse $\tan(\tan^{-1}x) = x$ for all x in the interval $(-\infty, \infty)$. $\tan^{-1}(\tan\theta) = \theta$ for all θ in the interval $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$.



Do not get into the habit of using a calculator to evaluate the composition of trigonometric expressions as it is possible to get false results.

OBJECTIVE 2: Evaluating Composite Functions Involving Inverse Trigonometric Functions of the Form $f \circ g^{-1}$ and $f^{-1} \circ g$