

In all homework problems, it is not sufficient to show only the answers. *You must show your work.* These exercises are based on Chapter Three.I and Three.II from the text.

1. Use these matrices for this exercise.

$$A = \begin{bmatrix} 1 & 3 & -1 \\ 0 & 1 & 2 \end{bmatrix} \quad B = \begin{bmatrix} 2 & 2 \\ -1 & 0 \end{bmatrix} \quad C = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 1 & 1 \\ 2 & -2 & 3 \end{bmatrix} \quad D = \begin{bmatrix} 0 & 0 \\ 4 & 0 \end{bmatrix}$$

- (a) Find  $-3A$ ,  $2A + 3C$  and  $2B - 5D$ , or state “not defined.”
- (b) There are 16 possible ways to multiply two of these matrices together, including multiplying a matrix by itself. Which of the possible matrix products are not defined?
- (c) Compute  $AB$  and  $AC$ , or state “not defined.”
2. Let  $A = \begin{bmatrix} 2 & 3 \\ -1 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 9 \\ -3 & k \end{bmatrix}$ . What value of  $k$ , if any, will make  $AB = BA$ ?
3. Let  $A = \begin{bmatrix} 3 & -6 \\ -1 & 2 \end{bmatrix}$ ,  $B = \begin{bmatrix} -1 & 1 \\ 3 & 4 \end{bmatrix}$ , and  $C = \begin{bmatrix} -3 & -5 \\ 2 & 1 \end{bmatrix}$ . Verify that  $AB = AC$ , even though  $B \neq C$ .
4. Show how to use matrix multiplication to bring this matrix to reduced row echelon form.

$$\begin{bmatrix} 2 & 1 & 4 & -1 \\ 1 & 3 & 10 & 8 \\ -1 & 2 & 3 & 7 \end{bmatrix}$$

5. Find the inverse or show the inverse does not exist for each of the following matrices.

$$(a) A = \begin{bmatrix} 1 & 0 & -2 \\ -3 & 1 & 4 \\ 2 & -3 & 4 \end{bmatrix} \quad (b) B = \begin{bmatrix} 1 & 2 & 1 \\ -4 & -7 & 3 \\ -2 & -6 & 4 \end{bmatrix}$$

6. For each space find the matrix changing a vector representation with respect to  $B$  to one with respect to  $D$ .

$$(a) V = \mathbb{R}^3, B = \mathcal{E}_3, D = \left\langle \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix} \right\rangle$$

$$(b) V = \mathbb{R}^3, B = \left\langle \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix} \right\rangle, D = \mathcal{E}_3$$

$$(c) V = \mathcal{P}_2, B = \langle x^2, x^2 + x, x^2 + x + 1 \rangle, D = \langle 2, -x, x^2 \rangle$$