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**Michael J Falk\*** ([michael.falk@nau.edu](mailto:michael.falk@nau.edu)), Dept. of Mathematics and Statistics, Northern Arizona University, Flagstaff, AZ 86011-5717. *The line geometry of resonance varieties.*

Let  $G$  be a matroid, and let  $A$  be the Orlik-Solomon algebra of  $G$  over a field  $R$ . We study the *resonance variety*  $\mathcal{R}_m$ , the set of elements of  $A^1 \cong R^n$  having  $(m + 1)$ -dimensional annihilator in  $A^1$ .

There is a combinatorial decomposition of  $\mathcal{R}_m$ , for  $R$  sufficiently large, in terms of neighborly partitions  $\Gamma$  of  $G$ . In this talk we focus on the geometry of these “combinatorial components.” Let  $\widehat{\mathcal{R}}_m$  be the projective image of  $\mathcal{R}_m$ . We show that the piece of  $\widehat{\mathcal{R}}_1$  arising from  $\Gamma$  is the carrier of a projective line complex, the intersection of linear line complexes determined by the subspace arrangement  $\mathcal{D}(G, \Gamma)$  of *directrices*.

Using this approach we answer in the *negative* a question posed by A. Suciu, whether the components of  $\mathcal{R}_m$  are linear for any (algebraically closed) field  $R$ . This negative answer contradicts the assertion made by the author in a recent preliminary report (AMS Abstracts Vol. 23, Issue 2, #978-14-94). For the underlying matroid of the Hessian arrangement, with  $R$  an algebraically closed field of characteristic three, we exhibit a component of  $\widehat{\mathcal{R}}_1$  which is an irreducible cubic hypersurface in  $\mathbb{P}^4$ . (Received August 18, 2002)