### Spring 2004

# MATH 7390-3: Stochastic Analysis and Advanced Topics

**Time:** MWF 1:40–2:30

Room: Lockett 113

### Prerequisite

Math 7311 (Real Analysis I) or equivalent

### Coverage

This course contains two parts: (1) basic theory of stochastic integration with applications to mathematical finance (which appeals to finance students and non-probability math graduate students), (2) advanced research topics for Ph.D. students (which I will outline in an overview for further independent study). Below are some items to be covered in this course:

- 1. Brownian motion
- 2. Construction of Brownian motion
- 3. Wiener integrals
- 4. Itô's integrals
- 5. Stochastic integrals for martingales
- 6. The Itô formula
- 7. Girsanov theorem
- 8. Stochastic differential equations
- 9. Arbitrage and option pricing
- 10. Black-Scholes analysis
- 11. Wiener-Itô decomposition theorem
- 12. White noise theory

#### References

The main references will be the first two books below, which are for part (1) of the coverage. For part (2) we will use the other two books.

- 1. Kuo, H.-H.: Introductory Stochastic Integration. (In preparation)
- 2. Oksendal, B.: Stochastic Differential Equations. 5th edition, Springer, 2000
- Kuo, H.-H.: Gaussian Measures in Banach Spaces. Lecture Notes in Math., Vol. 463, Springer-Verlag, 1975
- 4. Kuo, H.-H.: White Noise Distribution Theory, CRC Press, 1996

# Grading

The grade will be determined by homework assignments (65%) and the final exam (35%) with the tentative scale: A 85%; B 75%; C 65%

Professor H.-H. Kuo Office: Lockett 318 Telephone number: 578–1610 E-mail: kuo@math.lsu.edu Website: http://www.math.lsu.edu/~kuo