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**Instructions.** Do problems in space provided (continuing on back if necessary). This is a 100-point test.

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1. [5 points] Using the absolute-value symbol and  $<$  (or  $>$ ), express the following statement in mathematical symbols: “the distance from  $W$  to 3 is strictly greater than 5”.

2. [10 points] Describe as a union of intervals: the set of all  $x$  such that  $|2x - 9| \geq 100$ .

*In problems 3 and 4, let  $\ell$  be the line through  $(p, p^2)$  and  $(q, q^2)$ , where  $p$  and  $q$  are any real numbers.*

3. [5 points] Write the equation for  $\ell$  in slope-intercept form ( $y = mx + b$ ):

4. [10 points] Express as a function of  $p$ : the value that  $q$  must have in order for  $\ell$  to pass through  $(0, 1)$ :

5. [5 points] Write as a mathematical expression: “the average rate of change of  $f(x)$  on the interval from  $x = 6.9$  to  $x = 7$ .”

6. [5 points] Express as a limit: “the instantaneous rate of change of  $f(x)$  at  $x = 7$ .”
7. [10 points] An object falls from 256 feet, so its height after  $t$  seconds of falling is  $256 - 16t^2$  feet. At what time does it hit the ground? Express as a limit: the object’s instantaneous velocity when it hits the ground. Evaluate this limit.
8. [5 points] Explain the meaning of the expression “ $\lim_{x \rightarrow 3} f(x) = 5$ ” in plain English, *without* using the word “limit.”
9. [5 points] Explain the meaning of the expression “ $\lim_{x \rightarrow \infty} f(x) = 8$ ” in plain English, *without* using the word “limit.”
10. [5 points] Draw a graph of  $f$  to illustrate: “ $\lim_{x \rightarrow 2} f(x)$  does not exist because the one-sided limits are different.”

11. [5 points] Draw a graph of  $f$  to illustrate: “ $\lim_{x \rightarrow 2} f(x)$  does not exist because  $f$  has an asymptote.”

12. [5 points] Draw a graph of  $f$  to illustrate: “ $\lim_{x \rightarrow 2} f(x)$  does not exist because  $f$  oscillates.”

10. Find the limit if it exists. If it does not exist, explain why.

a. [5 points]  $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 3}$

b. [5 points]  $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x - 4}$

c. [5 points]  $\lim_{x \rightarrow 5} \frac{x^2 - 9}{x - 4}$

d. [5 points]  $\lim_{x \rightarrow 3} \frac{x^2 - 4}{x - 3}$

e. [5 points]  $\lim_{x \rightarrow 0} \cos \frac{1}{x}$

This page is for you to give me feedback about the course so far. PLEASE DETATCH THIS PAGE FROM YOUR TEST AND HAND IN SEPARATELY. You may submit this without a name, if you wish, or you may sign it.

Think about the following kinds of questions: Among the things we have done in class, what do you most like/not like? What kinds of things are you anxious to learn about? What kinds of work do you find most rewarding, *etc.* Do you have any concerns about the way we have been working?

Thank you for your feedback .