Quiz 09/05/2012

1. Suppose $f(x,y) = \frac{x^2}{4} + \frac{y^2}{9}$. Sketch the level set 1 = f(x,y). Sketch the graph z = f(x,y) and describe the shape of the graph in a sentence.

2. Suppose $z = x \sin(x y)$. Calculate the following:

$$\frac{\partial z}{\partial x} =$$
$$\frac{\partial z}{\partial y} =$$
$$\frac{\partial^2 z}{\partial y \partial x} =$$

3. Find the equation of the plane tangent to $z = y^2 - x^3$ at (1, 2, 3).

4. Suppose $z = x e^y$, x = f(t) and y = g(t). Use the Chain Rule to express the derivative of $\frac{dz}{dt}$ in terms of x, y, f'(t) and g'(t).