

1. Integrate: $\int_0^1 \int_0^{1+\cos x} \sqrt{x + \sin x} dy dx$.
2. Let R be the triangle with vertices at $(-1, 0)$, $(1, 0)$ and $(0, 1)$. Express $\iint_R f(x, y) dA$ as an iterated integral in each of the two possible orders of integration. Do not evaluate the integrals. (Note: in one order, it will be written as a sum of two iterated integrals.)
3. Draw the region of integration and rewrite the integral, changing the order of integration. (Do not evaluate the new integral.)

$$\int_0^2 \int_{x^2}^{2x} f(x, y) dy dx.$$

4. Let D be the disk of radius 1 about $(0, 0)$. Evaluate using polar coordinates:

$$\iint_D \sqrt{1 + x^2 + y^2} dA.$$

5. Find $\iiint_E 2yz dV$ where E is the region of space bounded by the vertical planes $x = 0$, $y = 0$ and $y = 2 - 2x$, bounded on the bottom by the x - y -plane and bounded on top by the surface $z = \sqrt{x + y}$.
6. Suppose E is the region in space bounded by the planes $z = 0$, $x = 0$, $y = 1$ and the surfaces $y = x^2$ and $y = z^3$. Find the limits when this integral is written in the indicated orders:
 - a. $\int_{?}^{?} \int_{?}^{?} \int_{?}^{?} f(x, y, z) dx dy dz$
 - b. $\int_{?}^{?} \int_{?}^{?} \int_{?}^{?} f(x, y, z) dz dx dy$
 - c. (Hard) How do you write this integral in the order $\int \int \int f(x, y, z) dy dz dx$?
7. Use spherical coordinates to compute $\iiint_E z dV$, where E is the region of space inside the cone $\phi = \frac{\pi}{4}$ and between the spheres $\rho = 1$ and $\rho = 2$.
8. Suppose a piece of wire has parametric representation $\gamma(t) = (\cos t, 2 \sin t)$, $t \in [0, \pi]$ and the density of the wire is $\delta(x, y) = xy$ (units of mass per unit length). What is the weight?