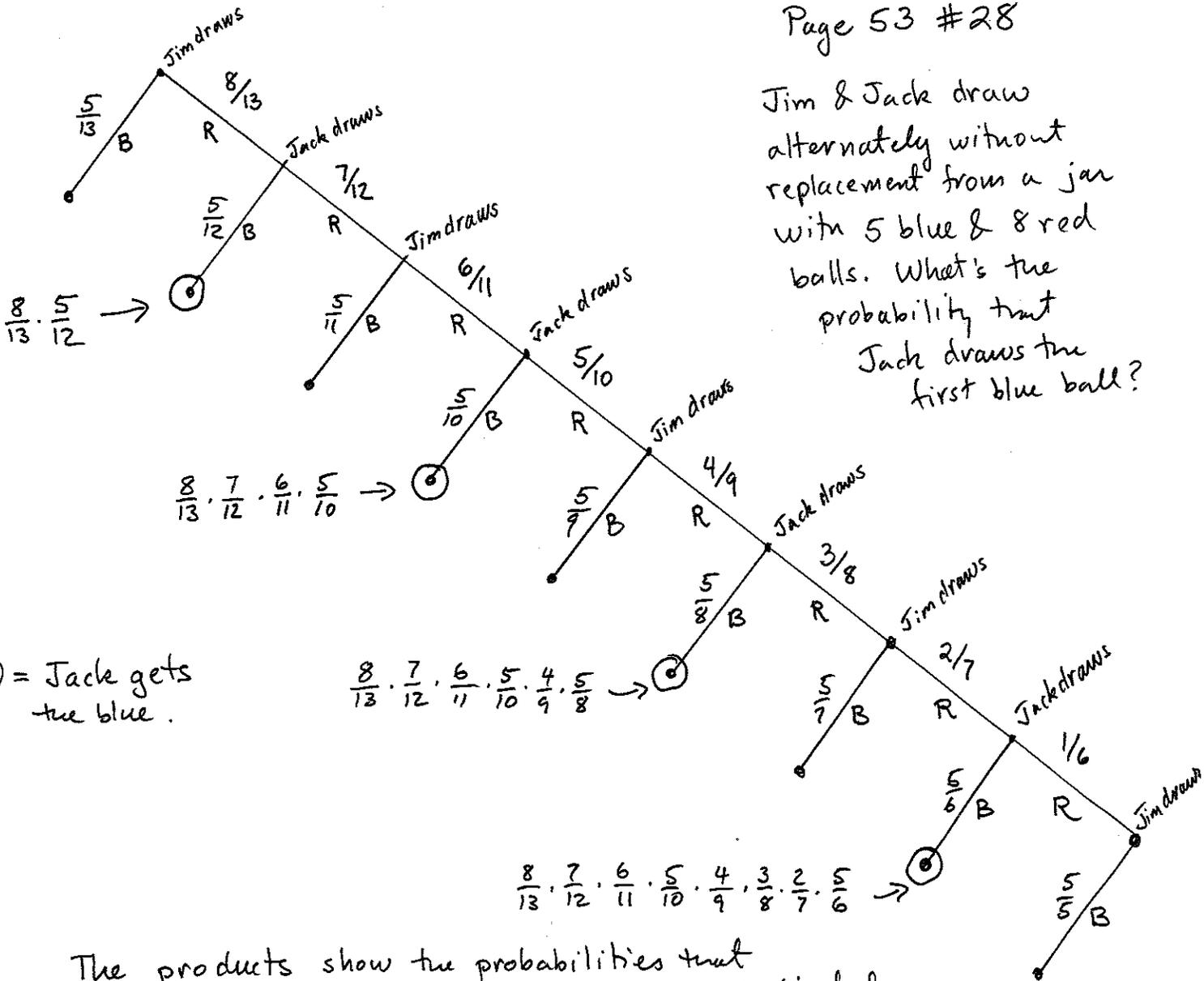


Jim & Jack draw alternately without replacement from a jar with 5 blue & 8 red balls. What's the probability that Jack draws the first blue ball?



⊙ = Jack gets the blue.

The products show the probabilities that the process terminates at the point indicated with the  $\rightarrow$ .

The probability that Jack gets the blue is the sum of these products =  $\frac{496}{1287} \approx 0.385392$

$$\begin{aligned}
 P(A \cap B) &= 1 - P(A^c \cup B^c) \\
 &= 1 - P(A^c) - P(B^c) + P(A^c \cap B^c) \\
 &\geq 1 - (1-a) - (1-b) \\
 &= a + b - 1 \\
 \therefore P(A|B) &= \frac{P(A \cap B)}{P(B)} \geq \frac{(a+b-1)}{b}
 \end{aligned}$$