

Instructions. Always include explanations, so that other readers can tell what you did and why you did it. Never write outside the box.

Celsius-Fahrenheit. Water freezes at 32 degrees Fahrenheit and it boils at 212 degrees Fahrenheit. Water freezes at 0 degrees Celsius and it boils at 100 degrees Celsius. If  $y$  is the temperature of an object in degrees Fahrenheit and  $z$  is the temperature of the same object in degrees Celsius, then what equations relate  $y$  and  $z$ ? How do you convert a temperature in degrees Fahrenheit to degrees Celsius? How do you convert a temperature in degrees Celsius to degrees Fahrenheit?

let  $y$  = temperature of an object in deg. F

$z$  = temp. of same object in deg. C

Freezing Point = 32 °F  
0 °C

Boiling Point = 212 °F  
100 °C

Celsius ( $z$ )	0	100
Fahrenheit ( $y$ )	32	212

$$\text{ROC} = \frac{\Delta y}{\Delta z} = \frac{212 - 32}{100 - 0} = \frac{180}{100} = 1.8$$

Celsius  
to Fahrenheit  $y = 1.8z + 32$

Fahrenheit to Celsius  $y = 1.8z + 32$

$$\begin{array}{r} y = 1.8z + 32 \\ -32 \\ \hline y - 32 = 1.8z \end{array}$$

$$\frac{(y - 32)}{1.8} = z$$

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$$y = \text{Temp in } {}^{\circ}\text{F}$$

$$z = \text{Temp in } {}^{\circ}\text{C}$$

Temperature in  ${}^{\circ}\text{F}(y)$  is equivalent to  $\frac{9}{5}$  of the Celsius Temperature ( $z$ ) plus 32.

$${}^{\circ}\text{F} \rightarrow {}^{\circ}\text{C}$$

Take the F value and subtract 32 from it. Then take the answer you get and multiply it by  $\frac{5}{9}$  to get the C value.

$${}^{\circ}\text{C} \rightarrow {}^{\circ}\text{F}$$

To convert from Celsius to Fahrenheit multiply  $\frac{9}{5}$  of the C value and add 32 to it. The answer gives you the value in  ${}^{\circ}\text{F}$ .

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First, you must should find the relationship/ratio of  ${}^{\circ}\text{F}$  to  ${}^{\circ}\text{C}$ . I will use the slope formula to do so. Let  $(y_1, z_1)$  be the coordinate so that  $(0, 32)$  and  $(100, 212)$  are our points:

$$m = \frac{y_2 - y_1}{z_2 - z_1} = \frac{212 - 32}{100 - 0} = \frac{180}{100} = \boxed{\frac{9}{5} \leftarrow \text{slope}}$$

Using this slope, choose one point to plug into point slope form.

$$y - y_1 = m(z - z_1) \quad \text{formula}$$

$$y - 32 = \frac{9}{5}(z - 0) \quad \begin{matrix} \text{Substitute slope \& point} \\ \text{either} \end{matrix}$$

$$y - 32 = \frac{9}{5}z - 180 \quad \begin{matrix} \text{Addition Prop} \\ +32 \qquad \qquad +212 \end{matrix}$$

$$\boxed{y = \frac{9}{5}z + 32} \quad \begin{matrix} \leftarrow \\ * \text{This is the formula that would} \\ \text{convert } {}^{\circ}\text{C to } {}^{\circ}\text{F.} \end{matrix}$$

To find the formula to convert  ${}^{\circ}\text{F}$  to  ${}^{\circ}\text{C}$ , solve for  $z$ .

$y = \frac{9}{5}z + 32$  subtract & multiply by reciprocal

$$-32 \quad \begin{matrix} \leftarrow \\ * \text{This is the formula that would} \\ \text{convert } {}^{\circ}\text{F to } {}^{\circ}\text{C.} \end{matrix}$$

$$\frac{5}{9}(y - 32) = \left(\frac{9}{5}z\right) \frac{5}{9}$$

$$\boxed{z = \frac{5}{9}y - \frac{160}{9}} \quad \leftarrow$$

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$$y = \text{temp. F.}$$

$$z = \frac{5}{9}(y - 32)$$

$$y = \frac{9}{5}z + 32$$

$$z = \text{temp. C.}$$

Example A:

$$32^{\circ}\text{F} = 0^{\circ}\text{C}$$

$(y) \qquad (z)$

$$y = \frac{9}{5}z + 32$$

$$32 = \frac{9}{5}(0) + 32$$

$$32 = 32 \checkmark$$

$$z = \frac{5}{9}(y - 32)$$

$$0 = \frac{5}{9}(32 - 32)$$

$$0 = \frac{5}{9}(0)$$

$$0 = 0 \checkmark$$

Example B:

$$212^{\circ}\text{F} = 100^{\circ}\text{C}$$

$(y) \qquad (z)$

$$z = \frac{5}{9}(y - 32)$$

$$100 = \frac{5}{9}(212 - 32)$$

$$100 = \frac{5}{9}(180)$$

$$y = \frac{9}{5}z + 32$$

$$212 = \frac{9}{5}(100) + 32$$

$$212 = \frac{900}{5} + 32$$

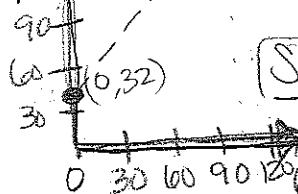
$$100 = 100 \checkmark$$

Deriving  
Formula

$$212 = 212 \checkmark$$

$$(y) \uparrow$$

(0, 32) (100, 212)



$$\text{Slope} \rightarrow \frac{212 - 32}{100 - 0} = \frac{180}{100} = \frac{18}{10} = \boxed{\frac{9}{5}}$$

$$y = mx + b$$
$$32 = \frac{9}{5}(0) + b$$

$$32 = b \checkmark$$

$$y = \frac{9}{5}x + 32$$

Then solve for  $C$  to get Celsius formula

$$F = \frac{9}{5}C + 32$$

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$$\text{Freezing pt of H}_2\text{O} \Rightarrow 32^{\circ}\text{F} = 0^{\circ}\text{C}$$

$$\text{Boiling pt of H}_2\text{O} \Rightarrow 212^{\circ}\text{F} = 100^{\circ}\text{C}$$

Let  $y$  be the temp. of an object in  $^{\circ}\text{F}$

$z$  be the temp. of an object in  $^{\circ}\text{C}$

$$m = \frac{212 - 32}{100 - 0} = \frac{180}{100} = \frac{9}{5}; b = 32$$

$$y = \frac{9}{5}z + 32$$

$$\boxed{y = \frac{9}{5}z + 32}$$

For  $z$ :

$$y = \frac{9}{5}z + 32$$

$$-32 \quad -32$$

$$\underline{[y - 32 = \frac{9}{5}z]} \cdot \frac{5}{9}$$

To convert a temperature in  $^{\circ}\text{C}$  to  $^{\circ}\text{F}$

$$^{\circ}\text{C} = \frac{5}{9}(F - 32)$$

$$\boxed{\frac{5}{9}(y - 32) = z}$$

To convert a temperature in  $^{\circ}\text{F}$  to  $^{\circ}\text{C}$

$$^{\circ}\text{F} = \frac{9}{5}\text{C} + 32$$

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~~$\frac{\Delta y}{\Delta z}$~~   
 $(F, C)$

$$(32, 0) \quad \frac{\Delta Y}{\Delta X} = \frac{100}{180} = \frac{10}{18} = \frac{5}{9}$$
$$(212, 100)$$

~~DOESN'T~~

$$z = \frac{5}{9}(y - 32)$$
$$y = \frac{9}{5}z + 32$$

$$z - 0 = \frac{5}{9}(y - 32)$$

or

$$y - 32 = \frac{9}{5}(x - 0)$$

$$y = \frac{9}{5}x + 32$$

1) To convert  $C$  to  $F$ , multiply by  $\frac{9}{5}$  then add 32.

2) To convert  $F$  to  $C$ , subtract 32 then multiply by  $\frac{5}{9}$

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$$y(f) = 32^{\circ} \text{ freezing point}$$

$$f(z) = 0^{\circ}$$

Baking point

$$f(y) = 212$$

$$f(z) = 100^{\circ}$$

By Routh

$$100z = 180y + 32$$

$$\frac{z}{y} = \frac{100}{180 + 32}$$

$$100y = 180z + 32$$

$$y = \frac{180z + 32}{100}$$

$$f(y) = \frac{180z}{100} + 32$$

$$= 1.8z + 32$$

$$f(z) = \frac{fy - 32}{1.8}$$

$$\text{Thus: } y = 1.8z + 32$$

$$z = \frac{y - 32}{1.8}$$

$$f(y) = 55^{\circ}F$$

$$f(z) = 55^{\circ}C$$

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Water freezes  $\rightarrow 32^{\circ}\text{F} \rightarrow 0^{\circ}\text{C}$

Water boils  $\rightarrow 212^{\circ}\text{F} \rightarrow 100^{\circ}\text{C}$

$y$  is temp in  $^{\circ}\text{F}$



$$*y = \frac{9}{5}z + 32$$

$z$  is temp in  $^{\circ}\text{C}$

$$*z = \frac{5}{9}(y - 32)$$

\*To convert a temperature from Fahrenheit to Celsius, plug in the degrees Fahrenheit for  $y$  and solve by subtracting 32 and then multiplying by  $\frac{5}{9}$ .

\*To convert a temperature from Celsius to Fahrenheit, plug in the degrees Celsius for the  $z$  and solve by  $\rightarrow$  multiplying by  $\frac{9}{5}$ , then adding 32.

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$y = \text{temp in Fahrenheit}$  &  $z = \text{temp in Celsius}$

let  $y_1 = 32$  and  $y_2 = 212$ . Also, let  $z_1 = 0$  &  $z_2 = 100$ . Then  
the rate of change is  $m = \frac{212 - 32}{100 - 0} = \frac{180}{100} = \frac{18}{10} = \frac{9}{5}$  and  $b = 32$ .

Therefore,  $y = \frac{9}{5}z + 32$  (or  $z = \frac{5}{9}(y - 32)$ )<sup>②</sup>. To convert Fahrenheit to Celsius use equation <sup>②</sup>. To convert Celsius to Fahrenheit degrees, use equation <sup>①</sup>. For example, let  $z = 100^\circ\text{C}$ .  
Converting to Fahrenheit yields

$$y = \frac{9}{5}(100) + 32 = 9 \cdot 20 + 32 = 180 + 32 \\ = 212^\circ\text{F}$$

Let  $y = 32^\circ\text{F}$ , then converting to Celsius yields  
 $z = \frac{5}{9}(32 - 32) = \frac{5}{9} \cdot 0 = 0^\circ\text{C}$ .

Using the formulas <sup>①</sup> and <sup>②</sup>, we found the boiling point and freezing point stated in the problem.

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$$y = {}^{\circ}\text{F} \quad z = {}^{\circ}\text{C}$$

$$y = \frac{5}{9}z + 32 \quad \text{or} \quad z = \frac{9}{5}(y - 32)$$

You convert a temperature in  ${}^{\circ}\text{F}$  to  ${}^{\circ}\text{C}$  by subtracting 32, then multiplying the remainder by  $\frac{5}{9}$ . For example, to convert  $212^{\circ}\text{F}$  to  ${}^{\circ}\text{C}$ , you first subtract  $212 - 32$  to get 180, then multiply  $180 \cdot \frac{5}{9}$  to get 100, which is the  ${}^{\circ}\text{C}$  equivalent of  $212^{\circ}\text{F}$ .

To convert from  ${}^{\circ}\text{C}$  to  ${}^{\circ}\text{F}$ , just solve the equation  $z = \frac{5}{9}(y - 32)$  for  $y$  (or  ${}^{\circ}\text{F}$ ) to obtain  $y = \frac{9}{5}z + 32$ . Again as an example, converting  $100^{\circ}\text{C}$  to  ${}^{\circ}\text{F}$  requires you first to multiply  $100 \cdot \frac{9}{5}$  (obtaining 180), then to add 32 to the product (resulting in 212—the equivalent of  $100^{\circ}\text{C}$  in  ${}^{\circ}\text{F}$ ).

Proof for freezing point:

$$\begin{aligned} y &= 32^{\circ}\text{F}, z = \frac{5}{9}(32 - 32) & z &= 0; y = \frac{9}{5}(0) + 32 \\ z &= \frac{5}{9}(0) & y &= 0 + 32 \\ z &= 0^{\circ}\text{C} & y &= 32^{\circ}\text{F} \end{aligned}$$

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$y = 1.8z + 32$  This is the linear equation converting Celsius to Fahrenheit. Since we know the freezing point of water is  $32^{\circ}\text{F} = 0^{\circ}\text{C}$ , and the boiling point is  $100^{\circ}\text{C} = 212^{\circ}\text{F}$ , we can find the slope of the line

$$y = mz + b \quad \text{as} \quad m = \frac{212 - 32}{100 - 0} = \frac{180}{100} = 1.8,$$

So  $y = 1.8z + b$ . Using the boiling point  $(100, 212)$ , we find  $212 = 1.8(100) + b \Rightarrow 212 - 180 = b \Rightarrow b = 32$ .

So  $y = 1.8z + 32$ .

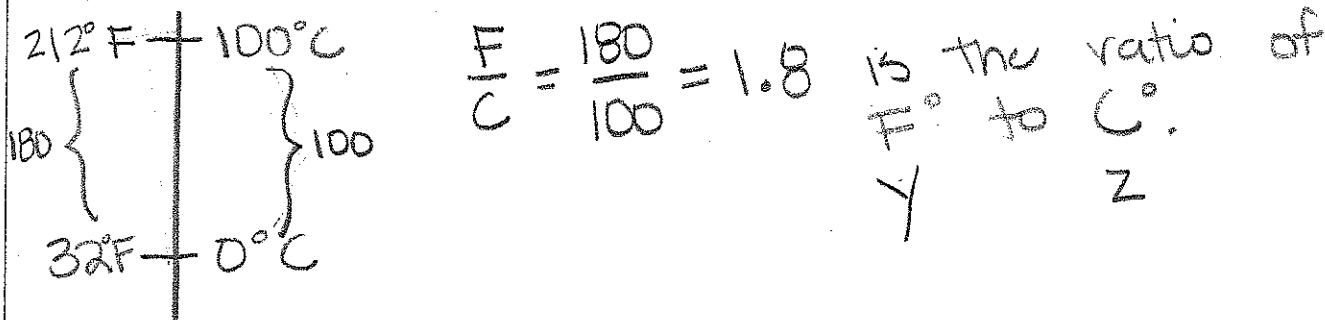
$z = \frac{y - 32}{1.8}$ . This is simply a manipulation of  $y = 1.8z + 32$ .

To convert from Fahrenheit to Celsius, you plug in your temperature in degrees Fahrenheit for  $y$  and evaluate.

To convert from Celsius to Fahrenheit, you plug in your temperature in degrees Celsius for  $z$  in  $y = 1.8z + 32$  and evaluate.

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$$y = 1.8z + 32 \rightarrow \text{use the ratio, but add 32 since } F^\circ \text{ starts at } 32^\circ \text{ for freezing when } C^\circ \text{ starts at } 0^\circ.$$
$$F^\circ = 1.8C^\circ + 32$$
$$\begin{array}{r} -32 \\ -\quad 32 \\ \hline \end{array}$$
$$\frac{F^\circ - 32}{1.8} = \frac{1.8C^\circ}{1.8}$$

$$C^\circ = \frac{F^\circ - 32}{1.8} \rightarrow z = \frac{y - 32}{1.8}$$

\* Convert  $F^\circ$  to  $C^\circ$  by subtracting 32 since the  $F^\circ$  scale starts at 32 when the  $C^\circ$  starts at 0. Then divide by the ratio 1.8.

\* Convert  $C^\circ$  to  $F^\circ$  by multiplying by the ratio 1.8 and then adding 32.

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The equations that relate  $y$  and  $z$  are as follows

Let  $y$  = temperature in degrees Fahrenheit

Let  $z$  = temperature in degrees Celsius

(0, 32) (0, 213) points on the line! (outside the box)  
(100, 212) (32, 373) calculations for  
slope & eq. of line

$$\left. \begin{array}{l} C(z) = \frac{5}{9}(y - 32) \\ C(z) = \frac{5}{9}y - \frac{160}{9} \end{array} \right\} \text{linear equation}$$

$\frac{5}{9}$  is the slope of the line and  $-\frac{160}{9}$  is the y-intercept

and  $F(y) = \frac{9}{5}z + 32$       } and  $\frac{9}{5}$  is the slope and 32 the y-intercept

To convert a temperature in degrees Fahrenheit to degrees Celsius

use:  
 $F(y) = \frac{9}{5}z + 32$  and solve for  $z$

To convert a temperature in degrees Celsius to degrees Fahrenheit

use

$C(z) = \frac{5}{9}(y - 32)$  and solve for  $y$ .

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Water Freezes @  $32^{\circ}\text{F} \approx 0^{\circ}\text{C}$   
Boils @  $212^{\circ}\text{F} \approx 100^{\circ}\text{C}$

$$\text{Know: } F = \frac{9}{5}C + 32$$

Need to derive this  
eqn.

$y$  = temperature of an object in  $^{\circ}\text{F}$

$z$  = temperature of same object in  $^{\circ}\text{C}$

Question: What eqn relate  $y$  &  $z$ ?  $\frac{9}{5}z + 32 = y$

How do you convert  $^{\circ}\text{F}$  to  $^{\circ}\text{C}$ ?  $^{\circ}\text{F} = \frac{9}{5}^{\circ}\text{C} + 32$

How do you convert  $^{\circ}\text{C}$  to  $^{\circ}\text{F}$ ?  $^{\circ}\text{C} = \frac{5}{9}(^{\circ}\text{F} - 32)$

Know from given:

- a)  $y = 32$  when  $z = 0$
- b)  $y = 212$  when  $z = 100$

$z + 32 = y$  if  $z = 0$ ,  $y = 32$  This fulfills part a) of given. But does not fulfill part b) of given.

?  $z + 32 = 212$  So what times  $^{\frac{100}{5}}$  and added to 32 will give 212 to fulfill part b)?

$$\begin{array}{r} ?(100) + 32 = 212 \\ -32 \quad -32 \end{array}$$

$$\begin{array}{r} ?(100) = 180 \\ 100 \quad 100 \end{array}$$

? =  $\frac{9}{5}$  Therefore, the final equations has to be:

$$\frac{9}{5}z + 32 = y$$

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$$y = {}^{\circ}\text{F} \quad (C) z = .56(y - 32)$$

$$(F)y = 1.8z + 32$$

$$K = z + 273$$

Water freezes @  $32^{\circ}\text{F}$

$$.56(32 - 32)$$

$$.56(0) = 0^{\circ}\text{C}$$

$$0^{\circ}\text{C} + 273 = 273^{\circ}\text{K}$$

Water Boils  $212^{\circ}\text{F}$

$$.56(212 - 32) = 100.8^{\circ}\text{C}$$

$$100.8 + 273 = 373.8^{\circ}\text{K}$$

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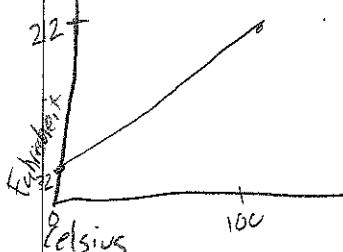
$$y = \text{Fahrenheit degrees} \quad z = \text{Celsius degrees}$$

$$\text{A) } y = \frac{9}{5}z + 32^\circ \quad \text{B) } z = \frac{5}{9}(y - 32^\circ)$$

A) To convert Celsius to Fahrenheit, first multiply the Celsius degree by the fraction  $\frac{9}{5}$ . Then take that product and add  $32^\circ$  degrees to it.

B) To convert Fahrenheit to Celsius, first subtract  $32^\circ$  from the given Fahrenheit degree. Then multiply that number by  $\frac{5}{9}$ .

To get A) is used linear algebra. I made the  $x$ -axis = Celsius and the  $y$ -axis = Fahrenheit degree. Then I plotted the point for the boiling point of water, which is  $100^\circ$  Celsius,  $212^\circ$  Fahrenheit. Then I plotted the point for the freezing point of water which is  $0^\circ$  Celsius,  $32^\circ$  Fahrenheit. Next I found the equation of the line ( $y = mx + b$ ). First the slope  $m = \frac{y_2 - y_1}{x_2 - x_1}$ . Using



the given points boiling and freeze respectively  $(100, 212), (0, 32)$

$$\frac{212 - 32}{100 - 0} = \frac{180}{100} = \frac{9}{5} = m$$

Now using knowledge about  $y = mx + b$ ,  $b$  is equal to the  $y$ -intercept. In other words

when Celsius is 0 what value does Fahrenheit have. Looking at the graph the  $y$ -intercept is  $32^\circ$  which is  $b$ . Then putting the new information into the equation of a line then  $y = \frac{9}{5}x + 32$ . Then relate the  $y$  and  $x$  axis to the given variables respectively the  $Fahrenheit = \frac{9}{5}Celsius + 32^\circ$

Instructions. Always include explanations, so that other readers can tell what you did and why you did it. Never write outside the box.

Celsius-Fahrenheit. Water freezes at 32 degrees Fahrenheit and it boils at 212 degrees Fahrenheit. Water freezes at 0 degrees Celsius and it boils at 100 degrees Celsius. If  $y$  is the temperature of an object in degrees Fahrenheit and  $z$  is the temperature of the same object in degrees Celsius, then what equations relate  $y$  and  $z$ ? How do you convert a temperature in degrees Fahrenheit to degrees Celsius? How do you convert a temperature in degrees Celsius to degrees Fahrenheit?

$$y = \text{temp in } {}^{\circ}\text{F}$$

$f$  = freezing pt

$$z = \text{temp in } {}^{\circ}\text{C}$$

$b$  = boiling pt

relate  
to  
f.  
 $y(f) = 32$

relate  
to  
b.  
 $y(b) = 212$

$z(f) = 0$

relate  
to  
b.  
 $z(b) = 100$

$$\begin{array}{r} 212 \\ - 32 \\ \hline 180 \end{array}$$

$$(1) y(f) = z(f) + 32$$

Using (1):

$$y(b) = x \cdot z(f) + 32$$

$$212 = x \cdot 100 + 32$$

$$180 = x \cdot 100$$

$$1.8 = x$$

$$y(t) = 1.8 z(t) + 32 \quad ; \quad z(t) = \frac{y(t) - 32}{1.8}$$

for some pt  $t$ .

To convert from  ${}^{\circ}\text{F}$  to  ${}^{\circ}\text{C}$ , subtract 32 then divide by 1.8.

To convert from  ${}^{\circ}\text{C}$  to  ${}^{\circ}\text{F}$ , multiply by 1.8 then add 32.

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Celsius-Fahrenheit. Water freezes at 32 degrees Fahrenheit and it boils at 212 degrees Fahrenheit. Water freezes at 0 degrees Celsius and it boils at 100 degrees Celsius. If  $y$  is the temperature of an object in degrees Fahrenheit and  $z$  is the temperature of the same object in degrees Celsius, then what equations relate  $y$  and  $z$ ? How do you convert a temperature in degrees Fahrenheit to degrees Celsius? How do you convert a temperature in degrees Celsius to degrees Fahrenheit?

$32^{\circ}\text{F}$  freeze

$0^{\circ}\text{C}$

$\text{F} \rightarrow \text{C}?$

$212^{\circ}\text{F}$  boils

$100^{\circ}\text{C}$

$\text{C} \rightarrow \text{F}?$

$$y = {}^{\circ}\text{F}$$

$$z = {}^{\circ}\text{C}$$

Pick 2 points of form  $(z, y)$

$$(0, 32)$$

$$(100, 212)$$

Find slope

$$\frac{212 - 32}{100 - 0} = \frac{180}{100} = \frac{9}{5}$$

$$y = \frac{9}{5}z + b \quad (\text{In terms of Fahrenheit})$$

$$y = \frac{9}{5}z + 32 \quad y\text{-intercept is } 32.$$

In terms of Celsius just solve for  $z$ .

$$y - 32 = \frac{9}{5}z$$

$$\frac{5}{9}(y - 32) = z$$