Math 7290 Fall 2016

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## Homework 2

Due: September 15, 2016

- 1. (Not to hand in) Exercise 10.13.
- 2. Assume that the characteristic of k is not 2. Prove that the set of unipotent elements in  $SL_2$  is isomorphic to the cone in  $\mathbb{A}^3$  given by  $x^2 + y^2 = z^2$ . (*Hint*: it might be easier to first show that it is isomorphic to the variety given by  $x^2 + yz = 0$  and then do a change of coordinates.)
- 3. Exercise 10.12.
- 4. Exercise 10.15(a)–(b) (you may use 10.14 without proof).
- 5. Exercise 10.16.