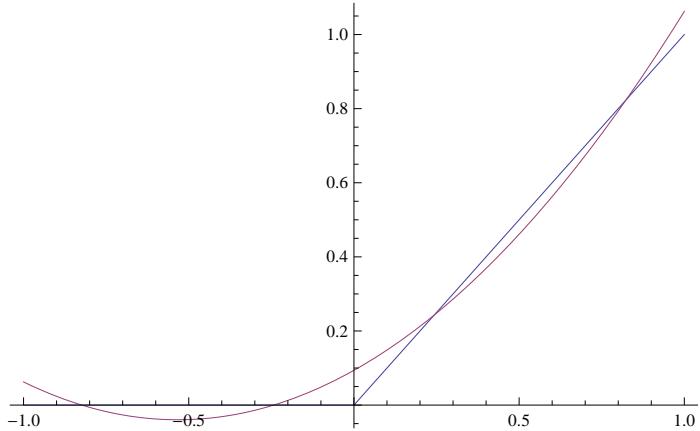


Here are the partial sums of the Fourier-Legendre series for  $f(x)=x$  on  $[0,1]$  and 0 on  $(-1,0]$ , using sums through P3 and through P7.

$$\text{Table}\left[(n+1/2) \int \text{LegendreP}[n, x] \frac{(x + \text{Abs}[x])}{2}, \{x, -1, 1\}\right], \{n, 0, 3\}$$

$$\left\{\frac{1}{4}, \frac{1}{2}, \frac{5}{16}, 0\right\}$$

$$\text{Plot}\left[\left\{\frac{(x + \text{Abs}[x])}{2}, \%. \text{Table}[\text{LegendreP}[n-1, x], \{n, \text{Length}[\%]\}]\right\}, \{x, -1, 1\}\right]$$



$$\text{Table}\left[(n+1/2) \int \text{LegendreP}[n, x] \frac{(x + \text{Abs}[x])}{2}, \{x, -1, 1\}\right], \{n, 0, 7\}$$

$$\left\{\frac{1}{4}, \frac{1}{2}, \frac{5}{16}, 0, -\frac{3}{32}, 0, \frac{13}{256}, 0\right\}$$

$$\text{Plot}\left[\left\{\frac{(x + \text{Abs}[x])}{2}, \%. \text{Table}[\text{LegendreP}[n-1, x], \{n, \text{Length}[\%]\}]\right\}, \{x, -1, 1\}\right]$$

